



## Running time (advanced version)

For each of the following algorithms:

- Compute the output of the function for example arguments.
- Determine the running time of the function.
- Figure out what the code is supposed to compute.
- If indicated, locate the bug. A bug refers to a mistake in the program, which may require several fixes.

### Foo

Use  $n$  for `v.size()`. There is one bug.

```
1 int foo(vector<int> const& v) {
2     int ans = 0;
3     for (int i = 0; i < v.size() - 1; ++i)
4         if (v[i] == v[i + 1])
5             ++ans;
6     return ans;
7 }
8 cout << foo({0,1,1,0,1,0,0,1}) << '\n';
9 cout << foo({3,3,2,2,2,9}) << '\n';
```

### Bar

Use  $n$  for `v.size()`.

```
1 int bar(vector<int> const& v) {
2     int ans = 0;
3     for (int i = 0; i < 1 << v.size(); ++i) {
4         int tmp = 0;
5         for (int j = 0; j < v.size(); ++j) {
6             if((i >> j) & 1) {
7                 tmp ^= v[j];
8             }
9         }
10        ans += tmp;
11    }
12    return ans;
13 }
14 cout << bar({3,5}) << '\n';
15 cout << bar({1,2,4}) << '\n';
```

### Baz

Use  $n$  for `v.size()`. There is one bug.

```
1 array<int, 4> bazar(vector<int> const&v, int l, int r) {
2     if (l == r) return {v[l], v[l], v[l], v[l]};
3     int m = (l+r)/2;
4     auto L = bazar(v, l, m);
5     auto R = bazar(v, m, r);
6     return {L[0] + R[0], max(L[1], L[0] + R[1]),
7             max(L[2] + R[0], R[2]), max({L[3], R[3], L[2] + R[1]})};
8 }
9 int baz(vector<int> const&v) {
10    assert(!v.empty());
11    return bazar(v, 0, v.size())[3];
12 }
13 cout << baz({-8,2,-1,3,-4,2}) << '\n';
14 cout << baz({-1,-1}) << '\n';
```



## Qux

There is one bug. The function is also very inefficient (asymptotically, not just by a constant factor), so optimize it.

```
1 const int p = 1e9+7;
2 int qux(int a, unsigned int n) {
3     if (n == 0) return 1;
4     if (n % 2) return qux(a, n-1) * a % p;
5     return qux(a, n/2) * qux(a, n/2);
6 }
7 cout << qux(2, 5) << '\n' << qux(3, p) << '\n';
```

## Flarp

Use  $n$  for  $v.size()$ . There are two bugs.

```
1 vector<int> flarp(vector<int> const& v) {
2     vector<int> ret(v.size()), s;
3     for (int e : v) {
4         while(!s.empty() && s.back() >= e) s.pop_back();
5         ret.push_back(s.back());
6         s.push_back(e);
7     }
8     return ret;
9 }
```

## Bongo

Use  $n$  for  $v.size()$ . There is one bug.

```
1 vector<int> bongo(vector<int> const& v) {
2     vector<int> bo(v.size(), 1);
3     for(int i = 0; i < n; ++i)
4         for(int j = 0; j < i; ++i)
5             if(a[j] < a[i])
6                 bo[i] += bo[j];
7     return accumulate(bo.begin(), bo.end(), 0);
8 }
```

## Snork

There is one bug.

```
1 int snorkel(int n, int i) {
2     if(i <= 1) return 1;
3     if(n % i == 0) return 1 + snorkel(i, i - 1);
4     else return snorkel(n, i - 1);
5 }
6 int snork(int n){
7     return snorkel(n, n-1);
8 }
9 cout << snork(25) << '\n' << snork(50) << '\n' << snork(210) << '\n';
```

## Garply

Assume that  $v.size() == 2^n$ .

```
1 vector<int> garply(vector<int> v, int n) {
2     for(int i = 0; i < n; ++i) {
3         for(int j = 0; j < v.size(); ++j)
4             if(((j >> i) & 1) == 0)
5                 v[j + (1<<i)] += v[j];
6     }
7     return v;
8 }
9 for(int e:garply({3,1,5,7}, 2) cout << e << "\n";
```